

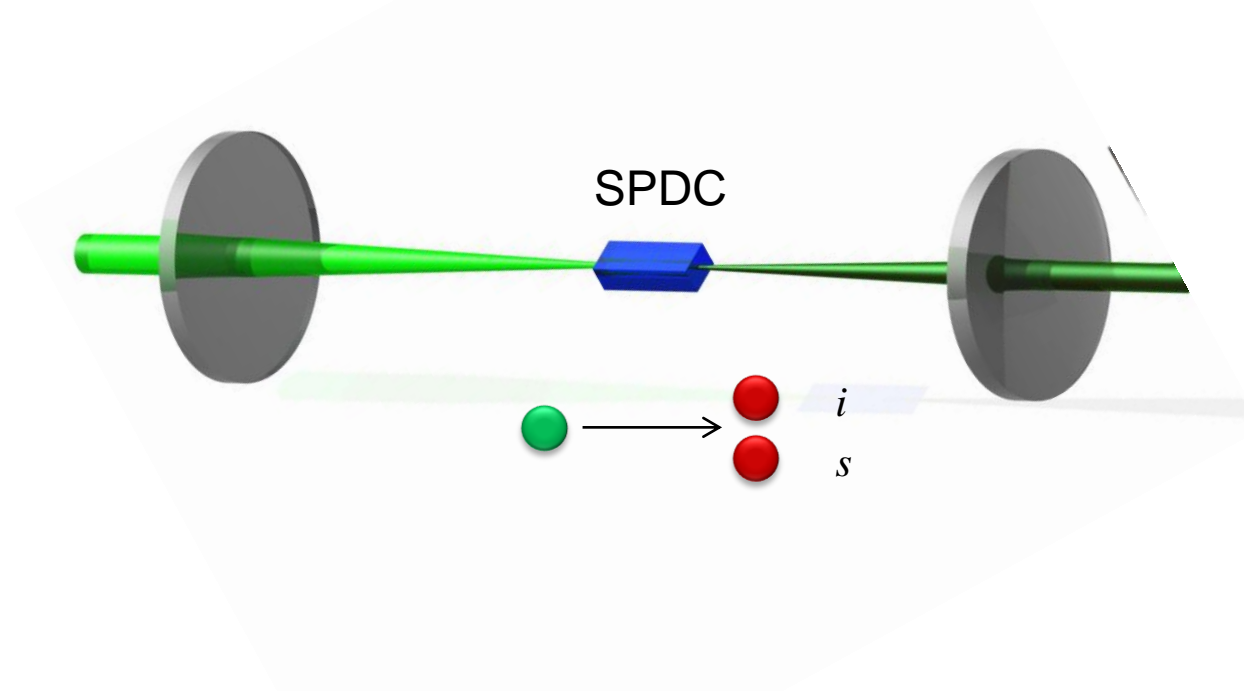


Broadband energy entangled photons and their potential for space applications

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University of Bern, Switzerland

Quantum Technology in Space, Malta, 29.03.2016

SPDC for quantum communication



Spontaneous parametric downconversion

- Easy
- High quality of states

Losses limit the maximal distance

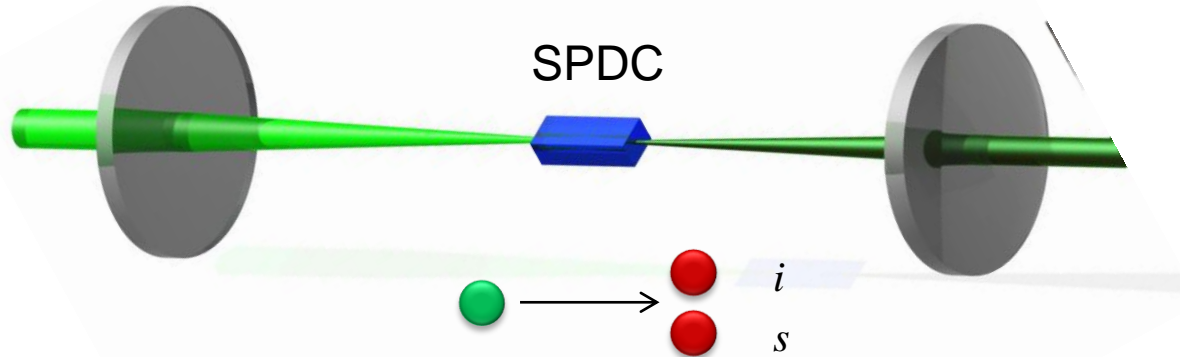
- Increase the pair production rate
- Increase the information capacity / pair



Outlook

- Energy-time photonic entanglement
- Experimental spectral manipulation
 - Quantum Information protocols, Bell Inequalities
 - Ultrafast measurements with CW light
- Conclusion, going to space

Photonic entangled qudits



- Polarization entanglement

$$|\phi^+\rangle = \frac{1}{\sqrt{2}} (|H\rangle_i |H\rangle_s + |V\rangle_i |V\rangle_s)$$

- Transverse momentum

$$|\psi\rangle = \int_{-\infty}^{\infty} d\mathbf{q}_i \int_{-\infty}^{\infty} d\mathbf{q}_s \Lambda(\mathbf{q}_i, \mathbf{q}_s) |1_{\mathbf{q}_i}\rangle_i |1_{\mathbf{q}_s}\rangle_s$$

- Energy entanglement

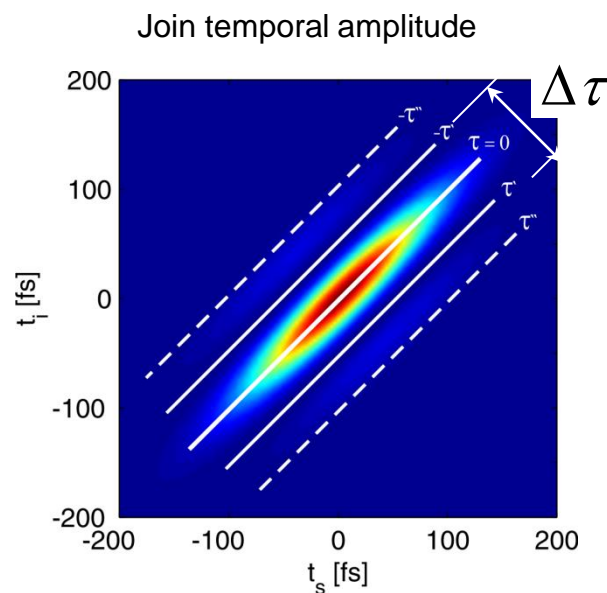
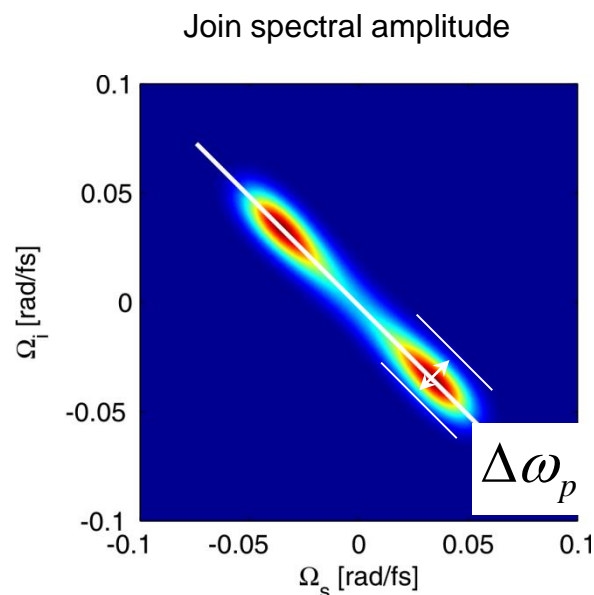
$$|\psi\rangle = \int_{-\infty}^{\infty} d\omega_i \int_{-\infty}^{\infty} d\omega_s \Gamma(\omega_i, \omega_s) |1_{\omega_i}\rangle_i |1_{\omega_s}\rangle_s$$

Broadband energy-entangled photons

Combine high temporal resolution with high energy resolution

$$|\psi\rangle = \int_{-\infty}^{\infty} d\omega_i \int_{-\infty}^{\infty} d\omega_s \Gamma(\omega_i, \omega_s) |1_{\omega_i}\rangle_i |1_{\omega_s}\rangle_s$$

$$\omega_p = \omega_s + \omega_i$$

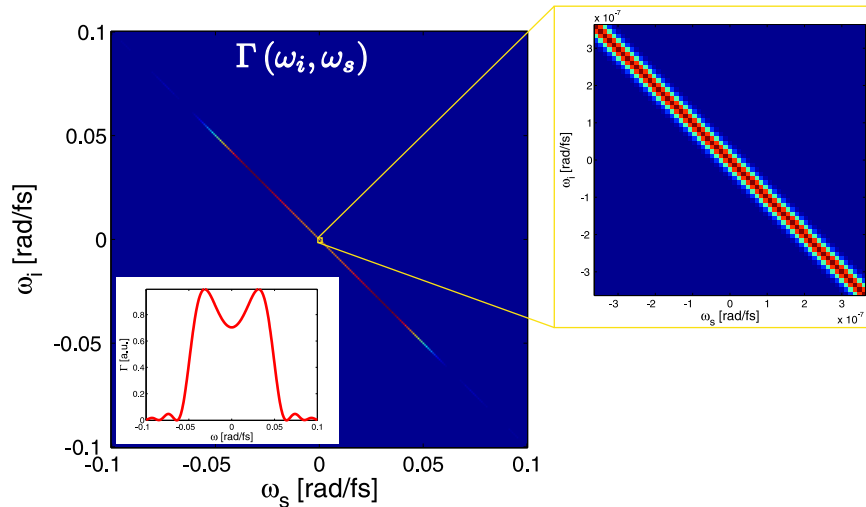


Classical light
Entangled light

$$\Delta\tau\Delta\omega > 1$$

$$\Delta\tau\Delta\omega_p \ll 1$$

Quantify the entanglement of the state $\Gamma(\omega_i, \omega_s)$



Entropy of the subsystem

$$A_i(\omega_i, \omega'_i) = \int_{-\infty}^{\infty} d\omega_s \Gamma(\omega_i, \omega_s) \Gamma(\omega'_i, \omega_s)$$

$$E(\mathbf{A}) = - \sum_{\lambda \in \sigma(\mathbf{A})} \lambda \log_2(\lambda)$$

Numerical computation

CW pump field \Rightarrow large discretized matrices: $m = 72 \times 10^6$

Compute E without diagonalization of \mathbf{A} : $E(\mathbf{A}) = 21.1 \pm 0.2$ ebits

\Leftrightarrow maximally entangled qudit with $d = 2^E \approx 2.2 \times 10^6$

T.P. Wihler, B. Bessire, A.S. Journal of Physics A, 47(24), 245201 (2014).

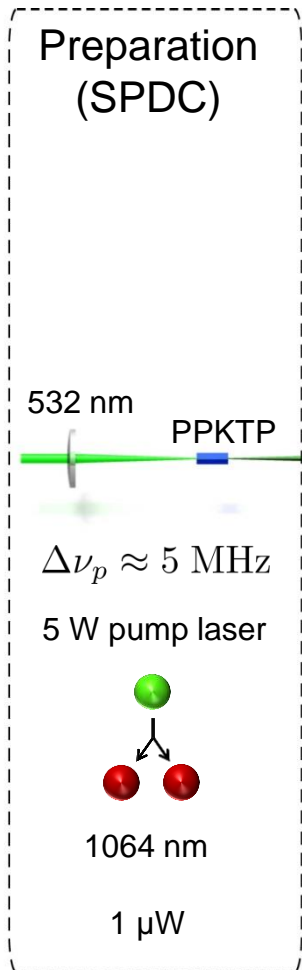
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Setup



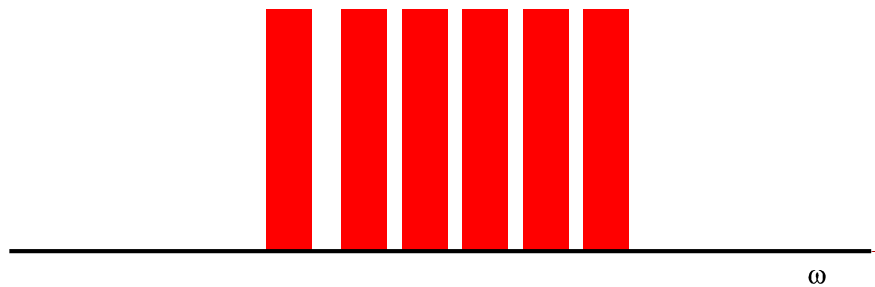
Detected signal after the SFG process:

$$S \propto \left| \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} d\omega_i d\omega_s \Gamma(\omega_i, \omega_s) M(\omega_i, \omega_s) \right|^2$$

\Rightarrow Sensitive to a phase in the SLM transfer function $M(\omega_i, \omega_s) = M^i(\omega_i) M^s(\omega_s)$

A. Pe'er, B. Dayan, A. A. Friesem, and Y. Silberberg, Phys. Rev. Lett. **94**, 073601 (2005)

Frequency-bins



Maximally entangled qutrit $|\psi\rangle^{(d)} = 1/\sqrt{3}(|0\rangle|0\rangle + |1\rangle|1\rangle + |2\rangle|2\rangle)$

In general $|\psi\rangle^{(d)} = 1/\sqrt{2 + \gamma^2}(|0\rangle|0\rangle + \gamma|1\rangle|1\rangle + |2\rangle|2\rangle)$

Quantum State tomography

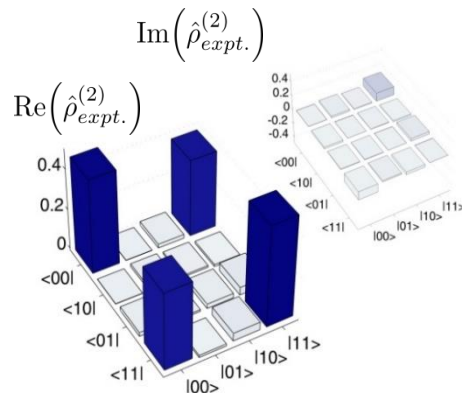
Detected signal is equivalent to the signal of a projective measurement

$$S \propto \left| \langle \chi | \psi \rangle^{(d)} \right|^2 \quad \text{with} \quad |\chi\rangle = \left(\sum_{j=0}^{d-1} u_j^{i*} |j\rangle_i \right) \left(\sum_{j'=0}^{d-1} u_{j'}^{s*} |j'\rangle_s \right)$$

Reconstruction of density matrices for maximally entangled qudits by Maximum Likelihood Estimation

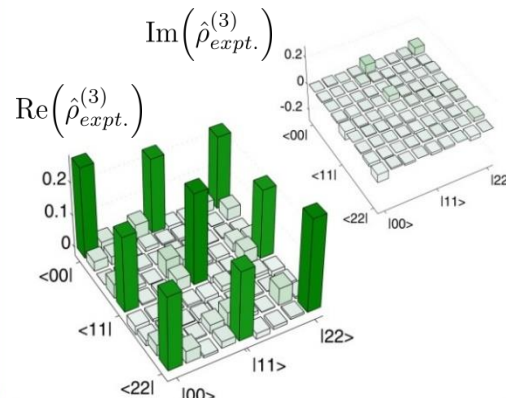
Qubit

$$F^{(2)} = 0.928 \pm 0.010$$



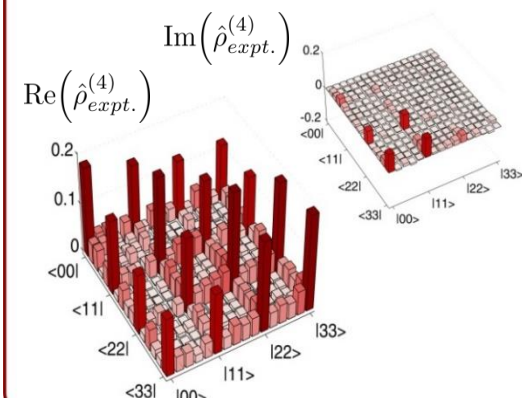
Qutrit

$$F^{(3)} = 0.855 \pm 0.010$$

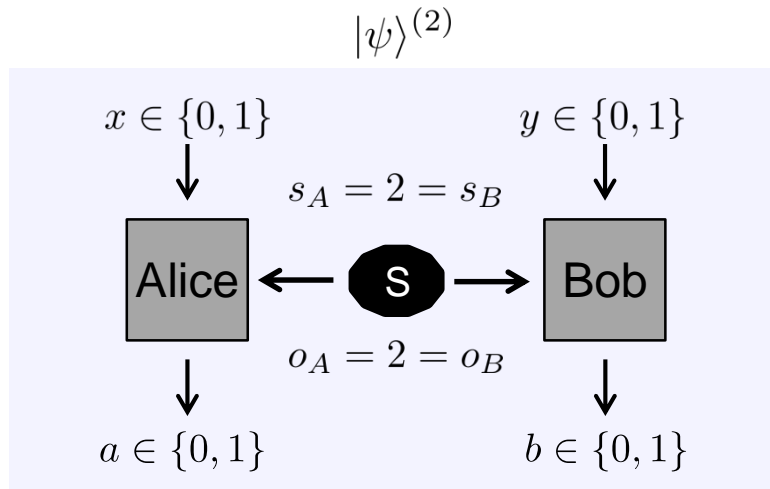


Ququart

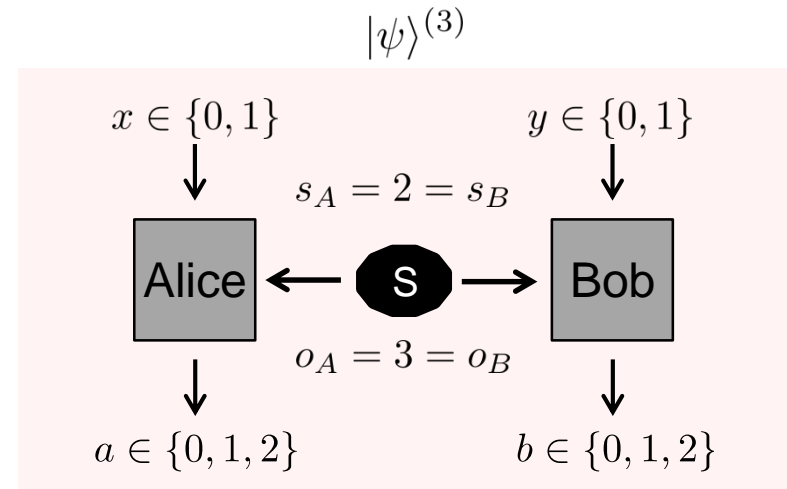
$$F^{(4)} = 0.781 \pm 0.018$$



Collins-Gisin-Linden-Massar-Popescu (CGLMP) inequality



B_{2222}



B_{2233}

$$I_{2,3}^{\text{CGLMP}} = +[P(A_1 = B_1) + P(A_1 = B_1 + 1) + P(A_2 = B_2) + P(A_2 = B_1)] \\ - [P(A_1 = B_1 - 1) + P(A_1 = B_2) + P(A_2 = B_2 - 1) + P(A_2 = B_1 - 1)] \leq 2$$

where the above probabilities are sums of joint probabilities given by

$$P(A_x = B_y + k) = \sum_{j=0}^{d-1} P(A_x = j, B_y = j + k \bmod d) = \sum_{j=0}^{d-1} P(j(j + k \bmod d) | xy)$$

CGLMP inequalities (with frequency-bins)

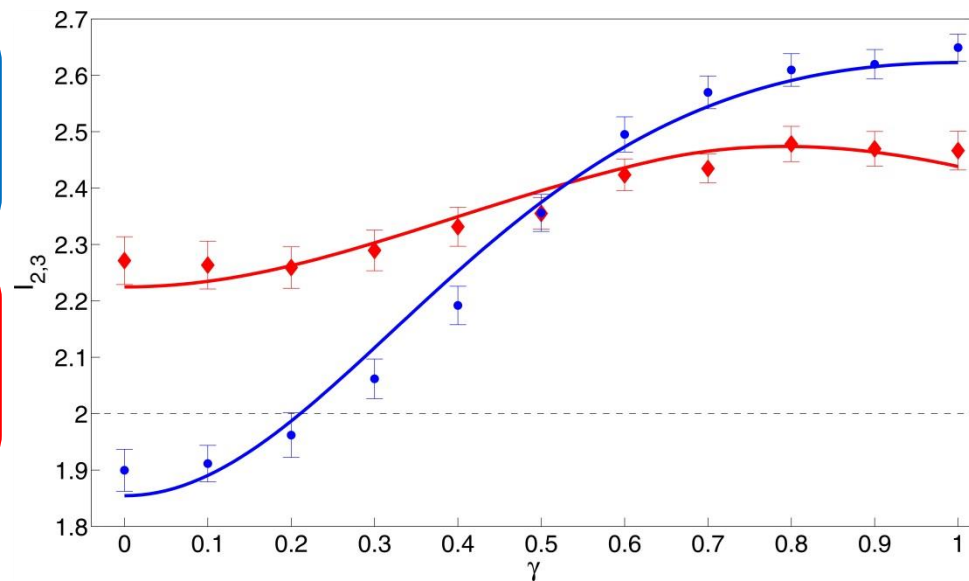
A *non*-maximally entangled qutrit state violates CGLMP stronger than a maximally entangled qutrit

2-qubit state with a γ :

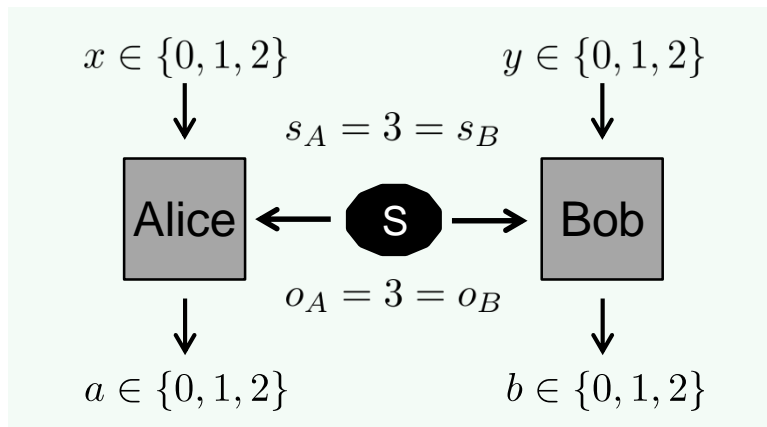
$$|\psi(\gamma)\rangle^{(2)} = \frac{1}{\sqrt{1+\gamma^2}}(|0\rangle_i|0\rangle_s + \gamma|1\rangle_i|1\rangle_s)$$

2-qutrit state with a γ :

$$|\psi(\gamma)\rangle^{(3)} = \frac{1}{\sqrt{2+\gamma^2}}(|0\rangle_i|0\rangle_s + \gamma|1\rangle_i|1\rangle_s + |2\rangle_i|2\rangle_s)$$

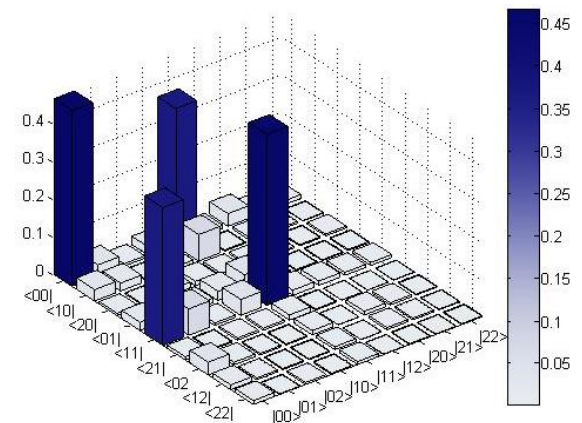
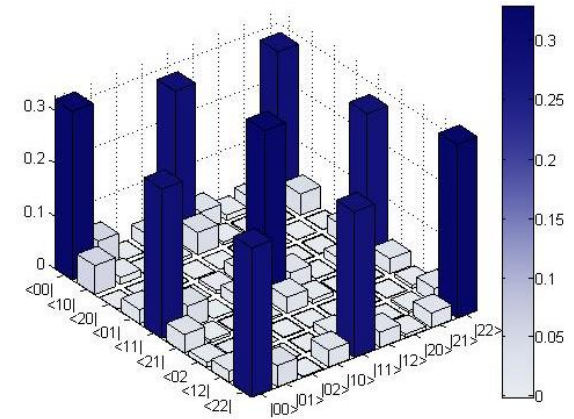


Multisettings Bell Scenario



B_{3333}

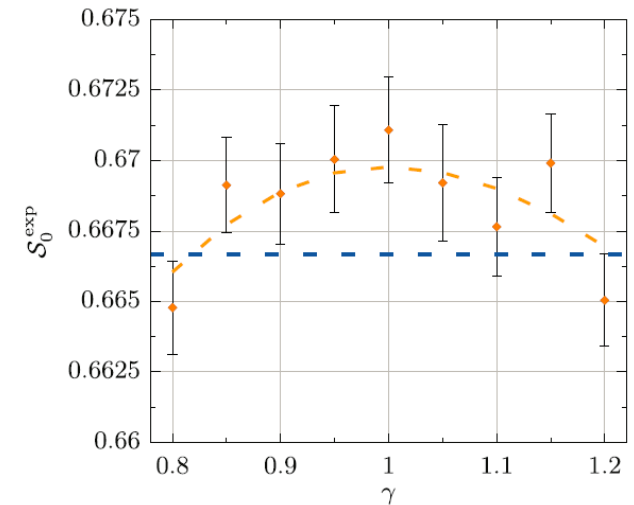
Some multisettings Bell inequalities can be maximally violated already with entangled two-qubit states



2-party, 3-Input, 3-Output Bell scenario

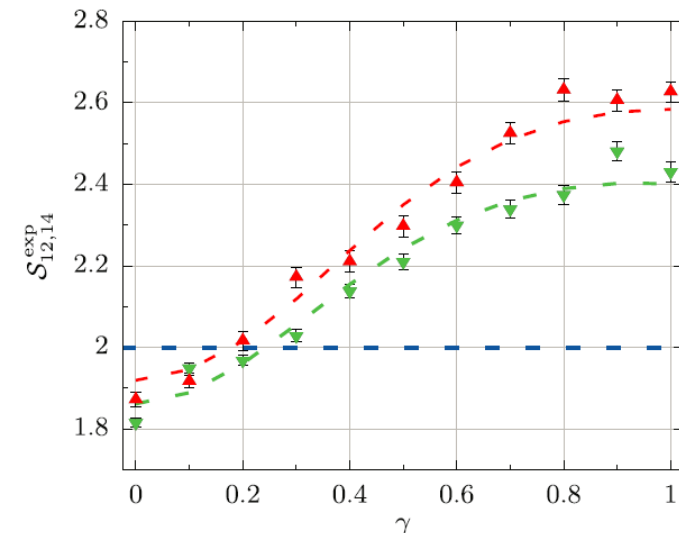
Maximally violated by maximally entangled qutrits

$$|\psi(\gamma, 1)\rangle = \frac{|0\rangle_A |0\rangle_B + \gamma |1\rangle_A |1\rangle_B + |2\rangle_A |2\rangle_B}{\sqrt{2 + \gamma^2}}$$



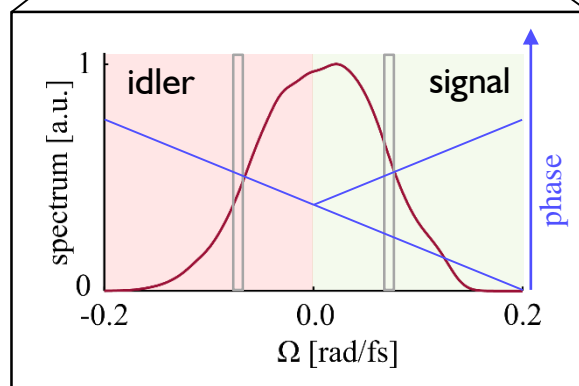
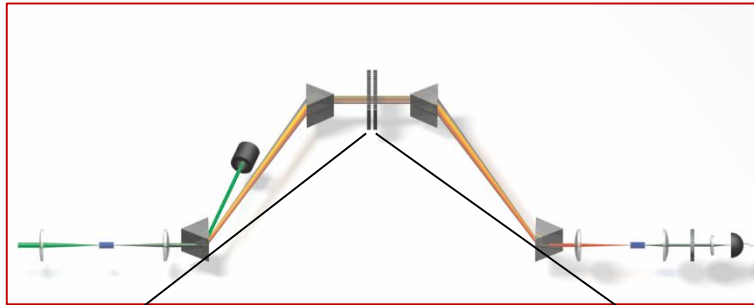
Maximally violated by entangled qubits

$$|\psi(\gamma, 0)\rangle = \frac{|0\rangle_A |0\rangle_B + \gamma |1\rangle_A |1\rangle_B}{\sqrt{1 + \gamma^2}}$$

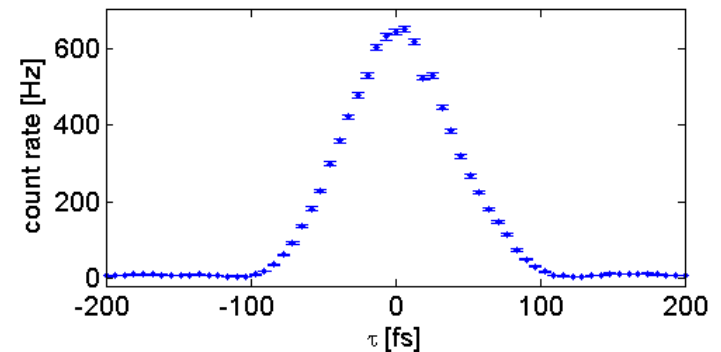
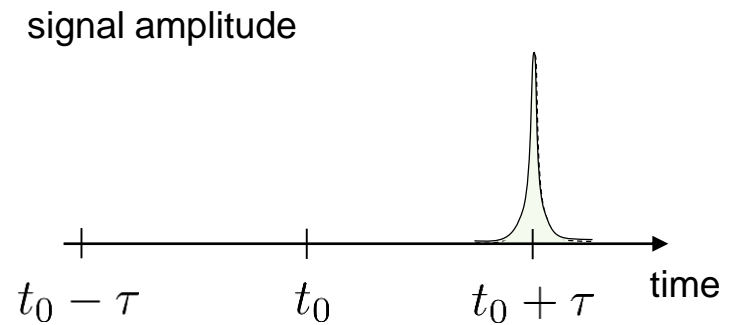
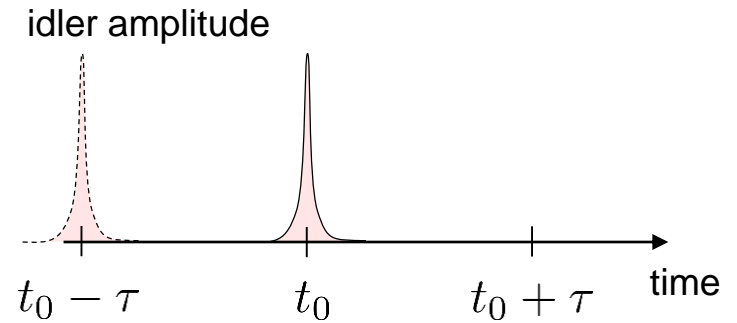


S. Schwarz, et al. NJP, 18(3), 035001 (2016)

Time shift between signal and idler

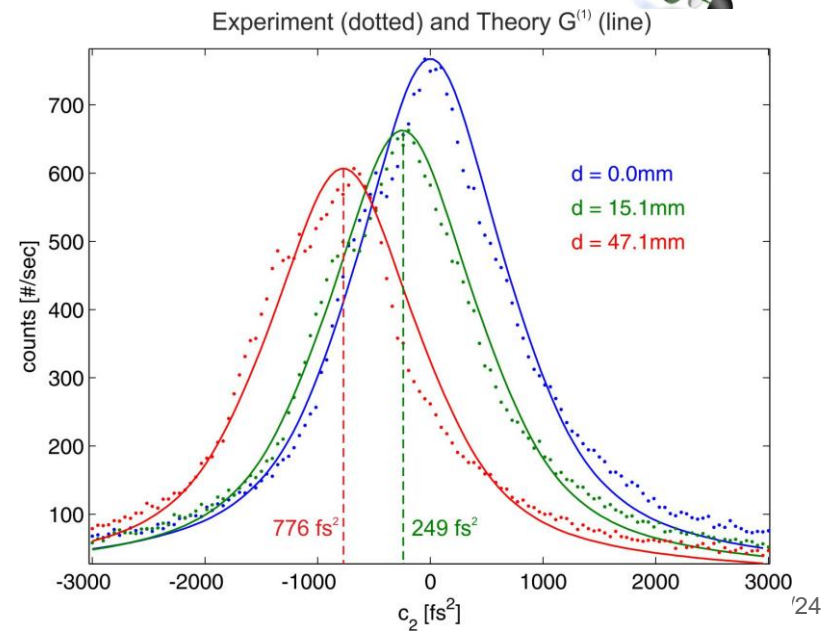
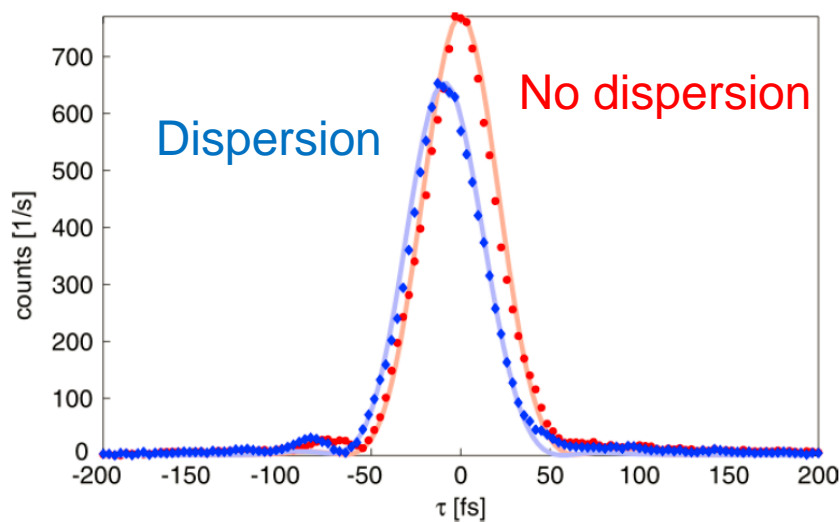
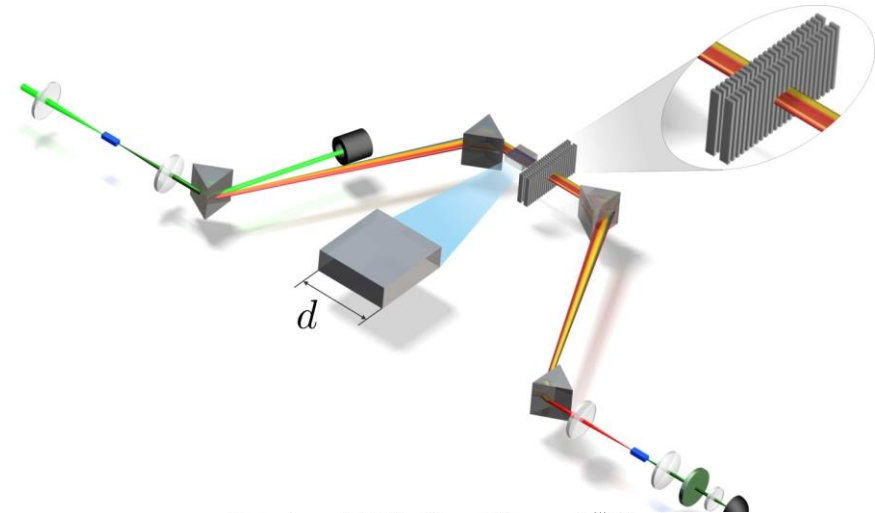


$$M(\Omega) = \exp\{-i|\Omega|\tau\}$$



Two photon correlation function $|\Psi(t)|^2$

- Fourier transform of $\Gamma(\omega)$
- Propagates like a fs pulse
... but CW



Dispersion cancellation by entanglement

Minimal broadening of the arrival time difference

minimal broadening

$$(\Delta\tau')^2 \geq (\Delta\tau)^2$$

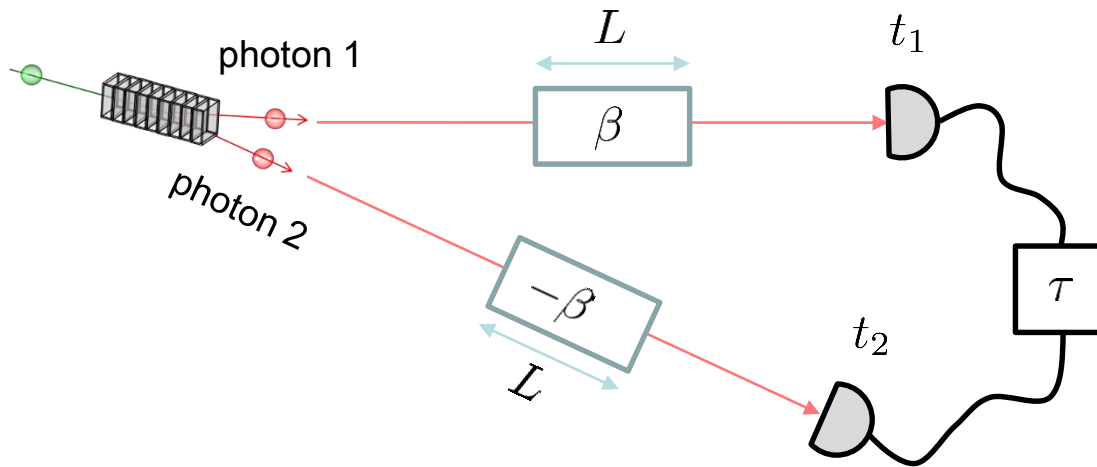


separable states

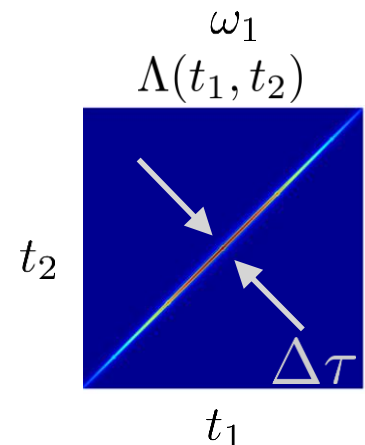
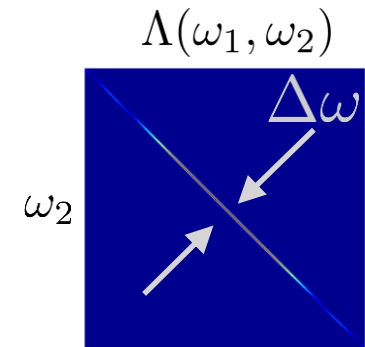
$$(\Delta\tau)^2(\Delta\omega)^2 \geq 1$$

$$\tau \doteq t_1 - t_2$$

$$\omega \doteq \omega_1 + \omega_2$$



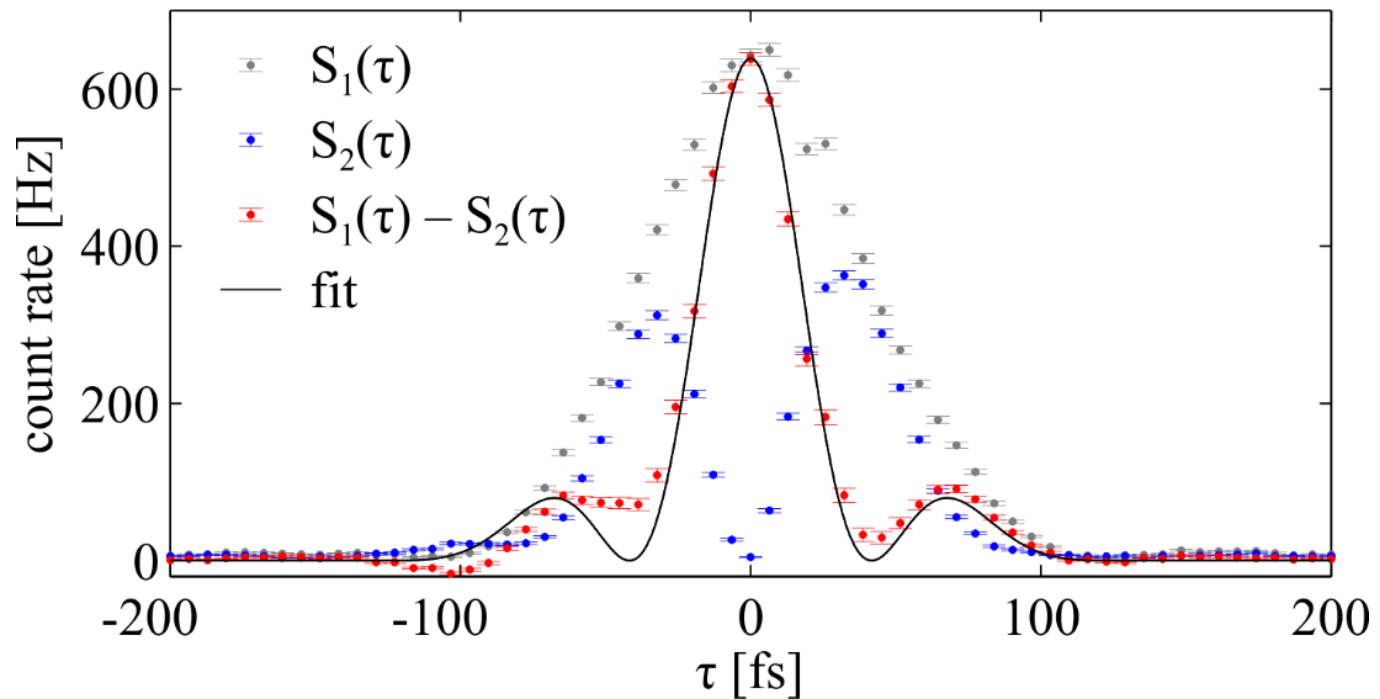
$\Delta\tau$ is the width of $G^{(2)}(t_1 - t_2)$



Measure of $G^{(2)}$

Target function is expressed by two signals

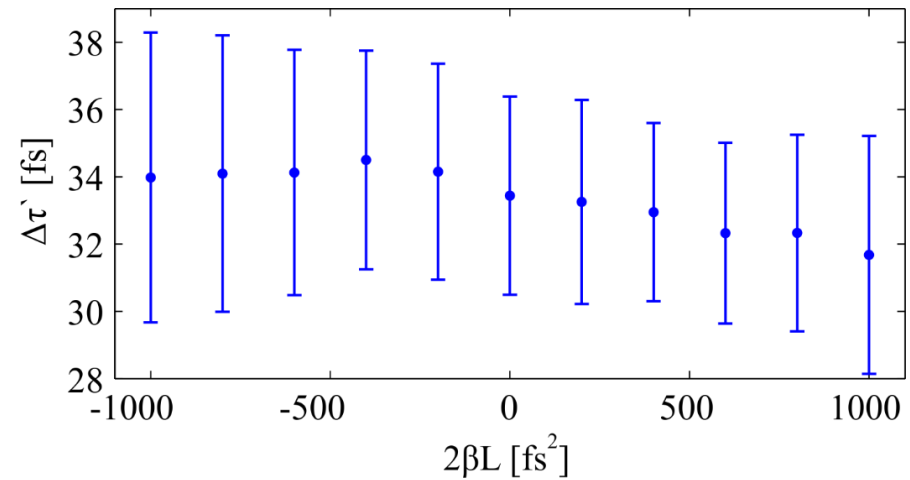
$$G^{(2)}(\tau) \propto S_1[M_1(\Omega)M_\beta(\Omega)] - S_2[M_2(\Omega)M_\beta(\Omega)]$$



Violation of classical inequality

No broadening observed

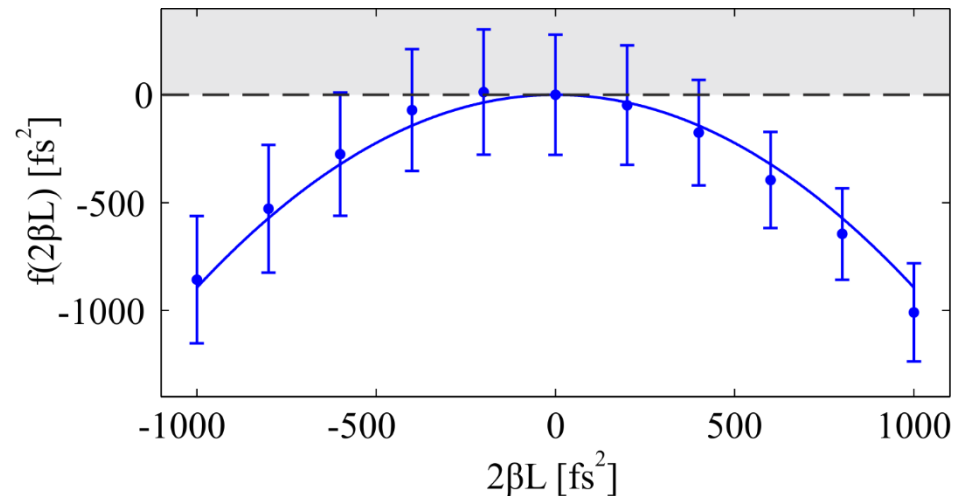
$$(\Delta\tau')^2 \geq (\Delta\tau)^2 + \frac{(2\beta L)^2}{(\Delta\tau)^2}$$



Violation of minimal broadening

$$f(2\beta L) \doteq (\Delta\tau')^2 - (\Delta\tau)^2 - \frac{(2\beta L)^2}{(\Delta\tau)^2}$$

$$\geq 0$$



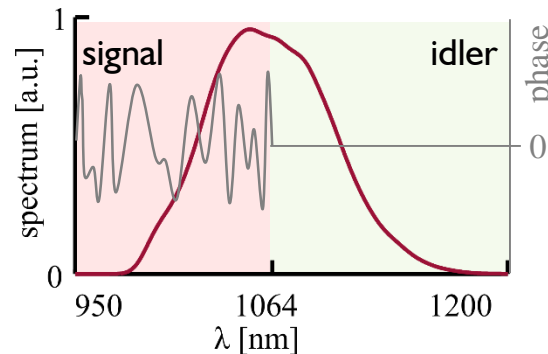
S.Lerch, et al., JOSA B, 50, 055505 (2017)

From entanglement to classical correlation

Entangled two-photon state

$$|\Psi_j\rangle = \int d\Omega \Lambda(-\Omega, \Omega) M_j(\Omega) M_j(-\Omega) |\Omega\rangle_s |-\Omega\rangle_i, \quad \hat{\rho}_j = |\Psi_j\rangle \langle \Psi_j|$$

Random phase at SLM \rightarrow destroy fixed phase relation (coherence) between signal and idler



State becomes a weighted mixture

Quantum correlations

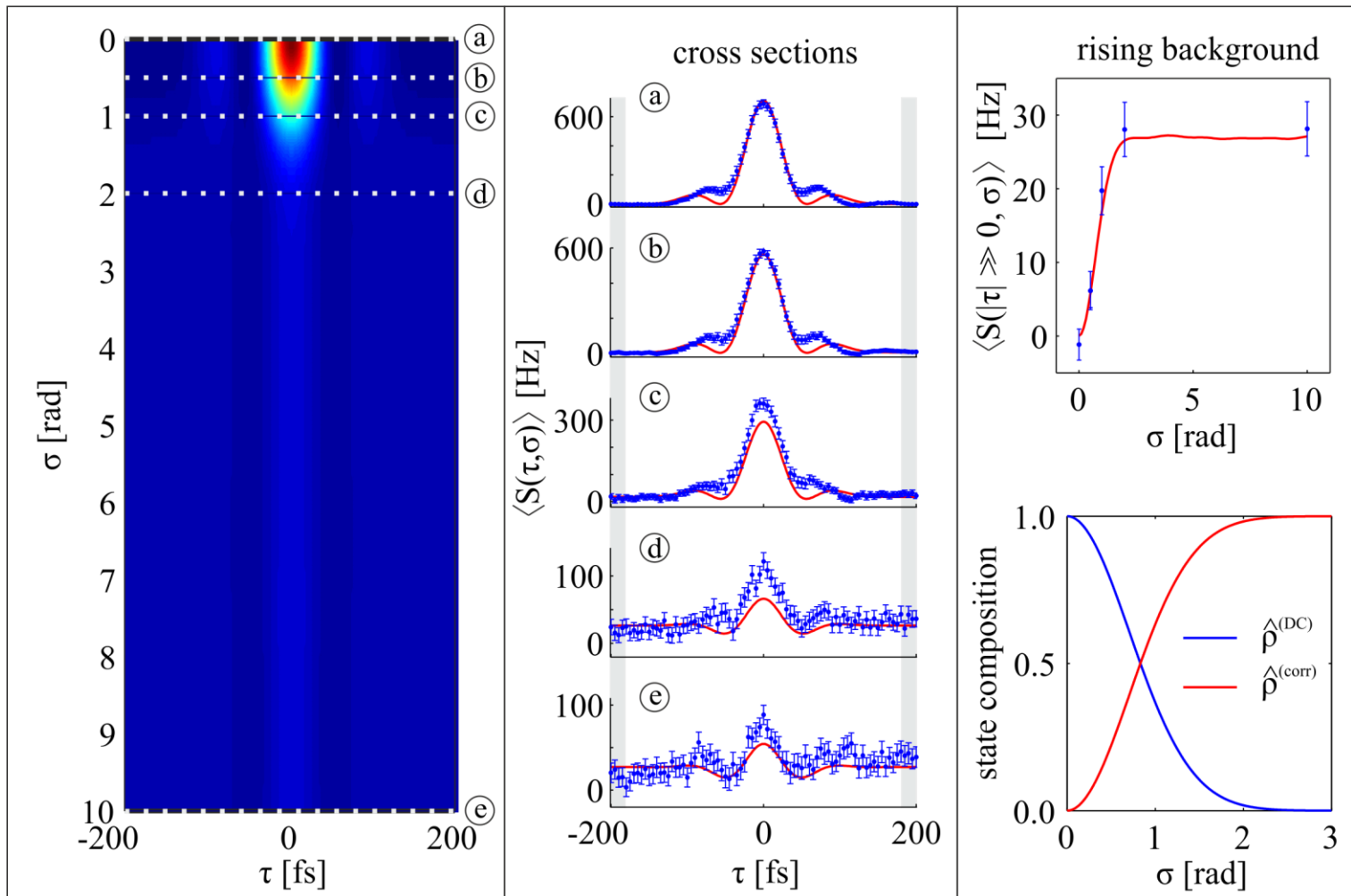
$$\hat{\rho} = e^{-\sigma^2} \left(\int d\Omega \Lambda(-\Omega, \Omega) |\Omega\rangle_s |-\Omega\rangle_i \right) \left(\int d\Omega' \Lambda(-\Omega', \Omega') \langle \Omega'|_s \langle -\Omega'|_i \right)$$

$$\left(1 - e^{-\sigma^2} \right) \left\{ \int d\Omega |\Lambda(-\Omega, \Omega)|^2 [|\Omega\rangle_s |-\Omega\rangle_i \langle -\Omega|_s \langle \Omega|_i + (1 - \delta(\Omega)) |\Omega\rangle_s |-\Omega\rangle_i \langle \Omega|_s \langle -\Omega|_i] \right\}$$

Classical correlations

From entanglement to classical correlation

Arrival time difference between signal and idler



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Conclusion, going to space

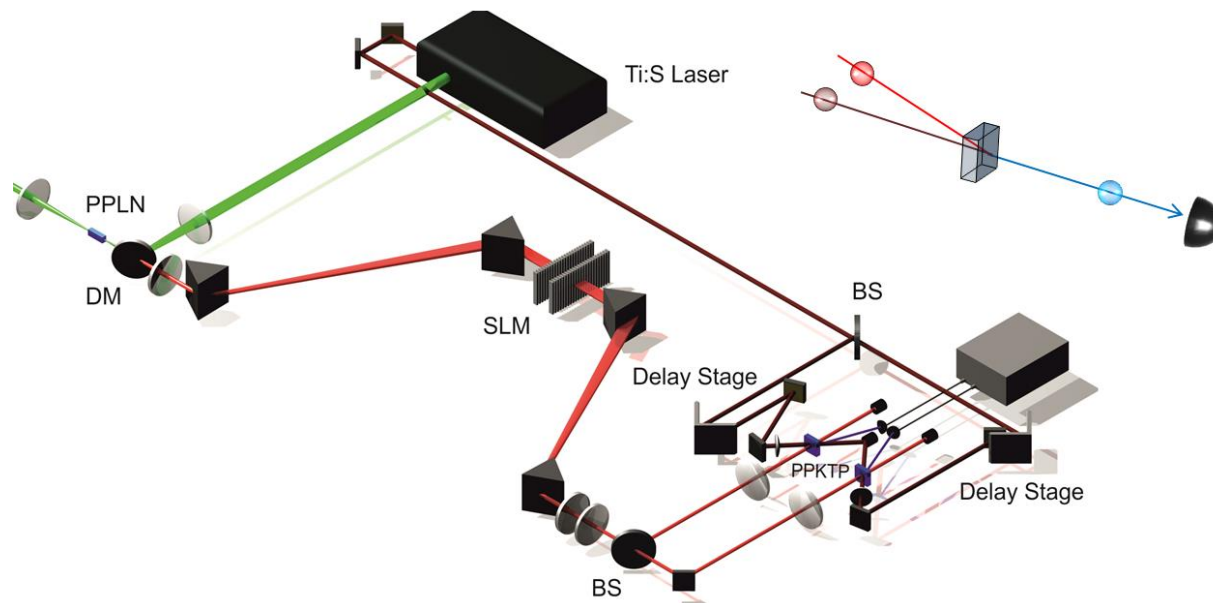
Broadband entangled photons

High temporal resolution

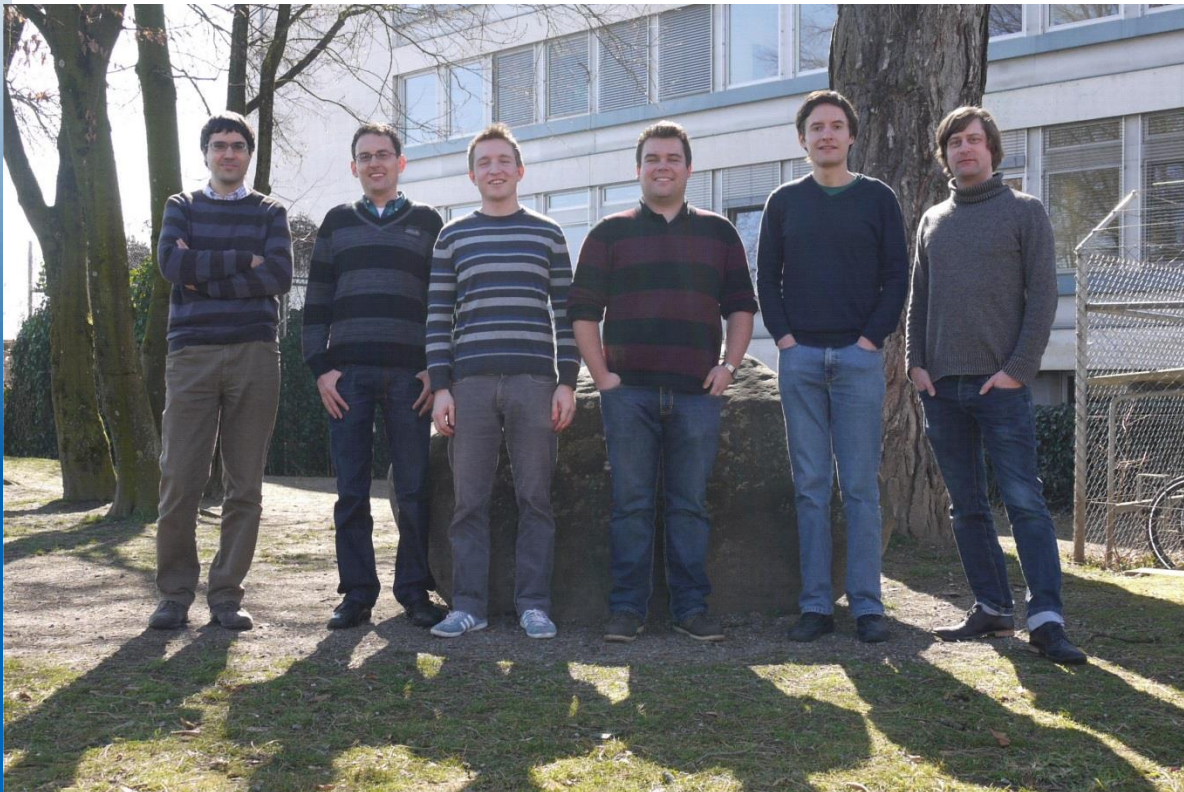
Large dimensional entanglement

Futur: High rate single photon detection with fs resolution

Non-local detection with fs timing resolution



Increase the duty cycle by space-time coupling



Thank you for your attention!

- ▷ B. Bessire
- ▷ C. Bernhard
- ▷ S. Lerch
- ▷ S. Schwarz
- ▷ M. Unternährer
- ▷ J. Kohn

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- F. Scheffold (Fribourg)
- Y.-C. Liang (Taiwan)